

# Part 3: Main Statistical Methods

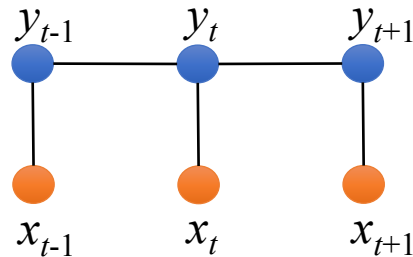
# Part 3.1: Graph-based Methods

# Graph-based Methods

- Training: Score  $\Leftrightarrow$  Correctness
- Decoding model score
  - enumerate all candidate structures; scoring each and selecting the highest scored structure

# Sequence Labeling Models

$$\text{CRF} \quad P(y_{[1:n]} | x_{[1:n]}) \propto \frac{1}{Z_{y_{[1:n]}}} \prod_{t=1}^n \exp \left( \begin{array}{l} \sum_j \lambda_j f_j(y_t, y_{t-1}) \\ + \sum_k \mu_k g_k(y_t, x_t) \end{array} \right)$$



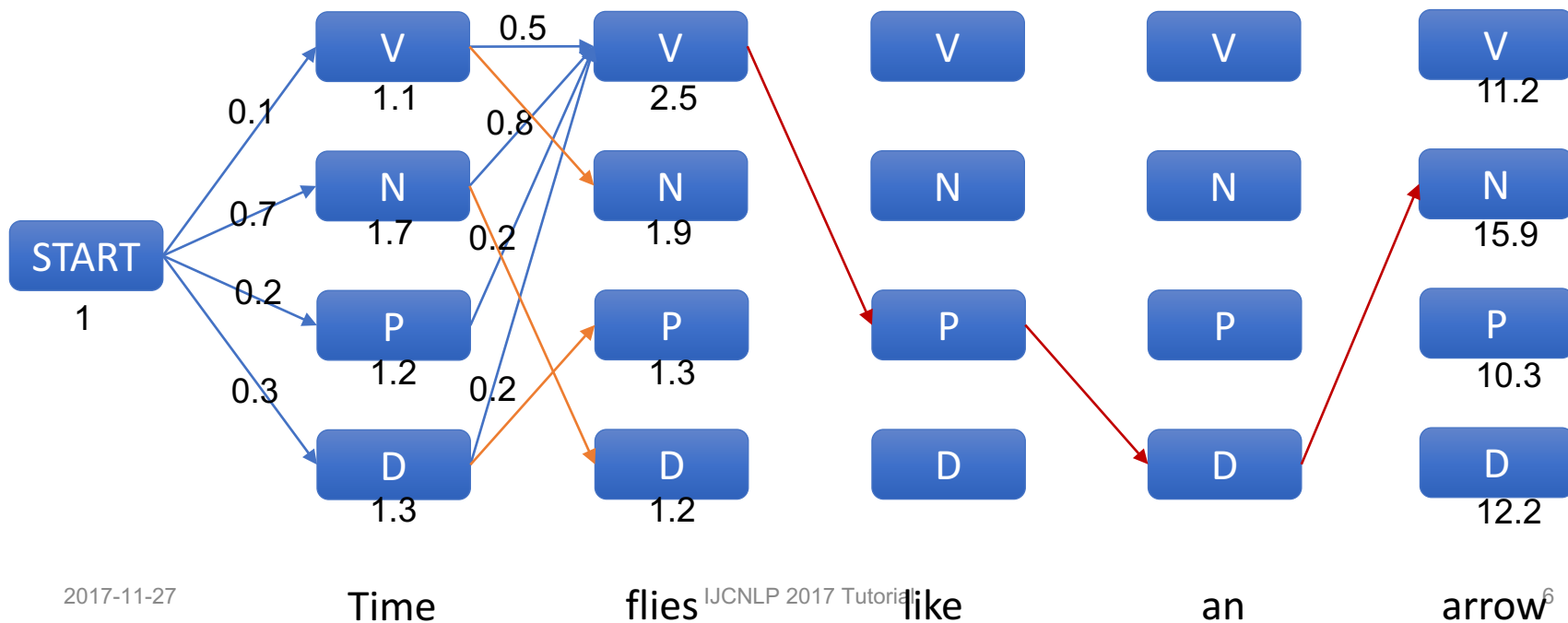
# CRF Decoding

$$\arg \max_{\mathcal{Y}_{[1:n]} \in \text{GEN}(x_{[1:n]})} \sum_{i=1}^n \mathbf{w} \cdot \mathbf{f}(x_{[1:n]}, y_i, y_{i-1})$$

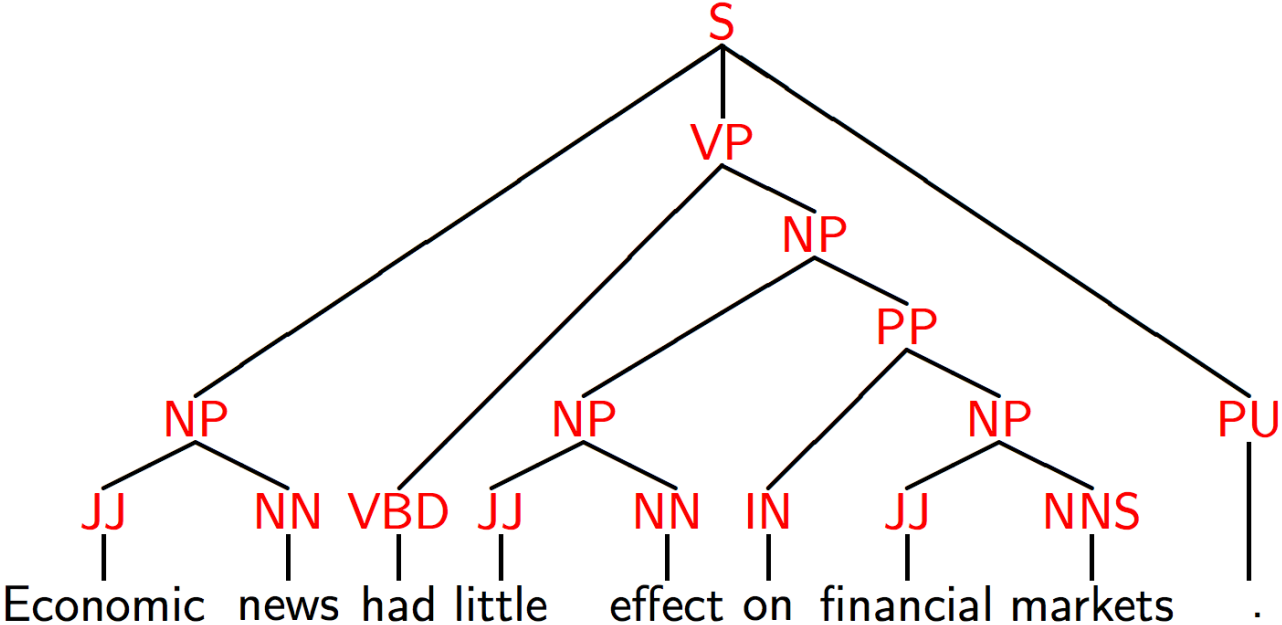
where  $\text{GEN}(x_{[1:n]})$  is all possible tag sequences

# Viterbi Algorithm

- Define a dynamic programming table
  - $\pi(i, y) = \text{maximum score of a tag sequence ending in tag } y \text{ at position } i$
- Recursive definition:  $\pi(i, y) = \max_t (\pi(i - 1, t) + \mathbf{w} \cdot \mathbf{f}(x_{[1:n]}, y, t))$



# Constituency Parsing

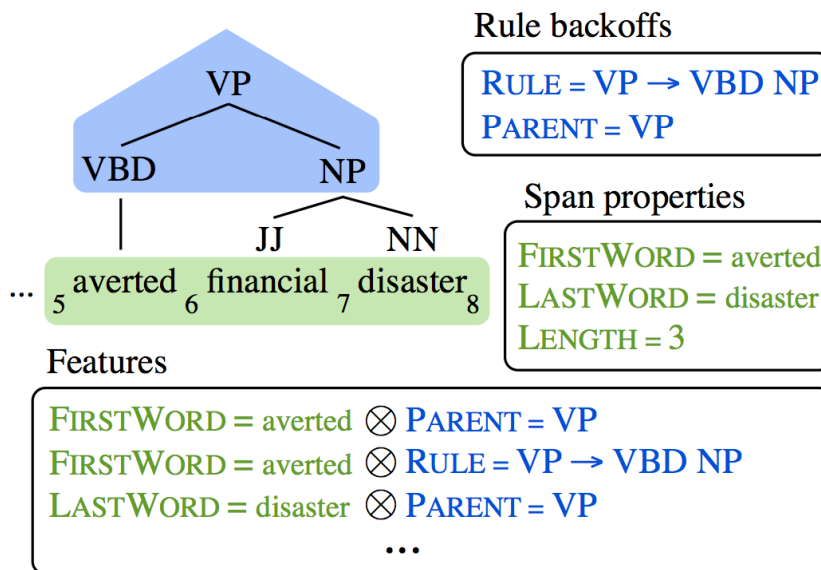


# Constituency Parsing with CRF

- Probability of a tree  $T$  conditioned on a sentence  $\mathbf{w}$

$$p(T|\mathbf{w}) \propto \exp \left( \theta^\top \sum_{r \in T} f(r, \mathbf{w}) \right)$$

- More features

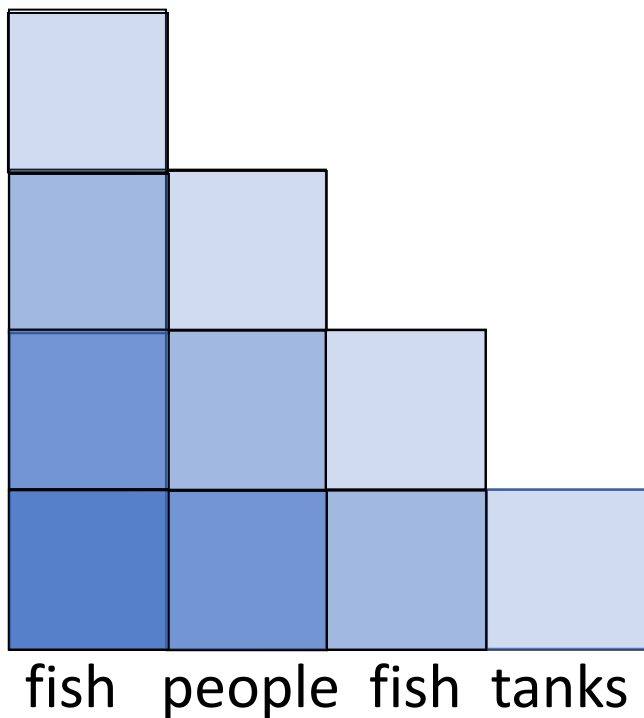


Hall D, Durrett G, Klein D (2014) Less grammar, more features. ACL.



# Chart-based Method

- E.g. Cocke–Younger–Kasami algorithm (CYK or CKY)
- A kind of Dynamic Programming



## PCFG

**Rule Prob  $\theta_i$**

$S \rightarrow NP VP$   $\theta_0$

$NP \rightarrow NP NP$   $\theta_1$

...

$N \rightarrow \text{fish}$   $\theta_{42}$

$N \rightarrow \text{people}$   $\theta_{43}$

$V \rightarrow \text{fish}$   $\theta_{44}$

# CKY Parsing Algorithm

**Input:** a sentence  $s = x_1 \dots x_n$ , a PCFG  $G = (N, \Sigma, S, R, q)$ .

**Initialization:**

For all  $i \in \{1 \dots n\}$ , for all  $X \in N$ ,

$$\pi(i, i, X) = \begin{cases} q(X \rightarrow x_i) & \text{if } X \rightarrow x_i \in R \\ 0 & \text{otherwise} \end{cases}$$

**Algorithm:**

- For  $l = 1 \dots (n - 1)$ 
  - For  $i = 1 \dots (n - l)$ 
    - \* Set  $j = i + l$
    - \* For all  $X \in N$ , calculate

$$\pi(i, j, X) = \max_{\substack{X \rightarrow YZ \in R, \\ s \in \{i \dots (j-1)\}}} (q(X \rightarrow YZ) \times \pi(i, s, Y) \times \pi(s + 1, j, Z))$$

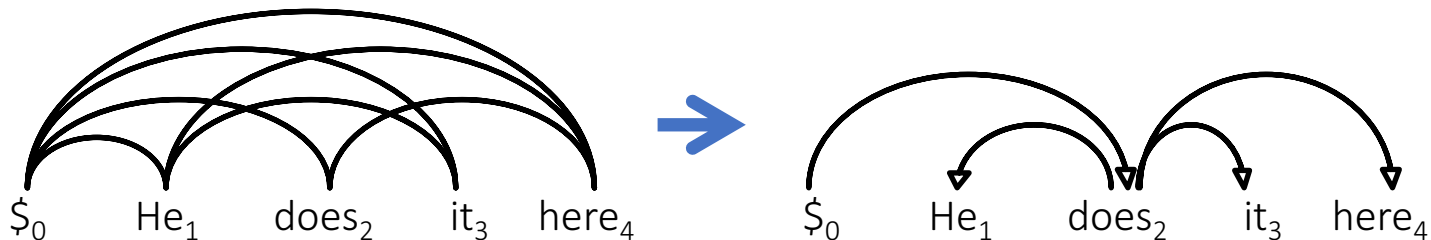
and

$$bp(i, j, X) = \arg \max_{\substack{X \rightarrow YZ \in R, \\ s \in \{i \dots (j-1)\}}} (q(X \rightarrow YZ) \times \pi(i, s, Y) \times \pi(s + 1, j, Z))$$

**Output:** Return  $\pi(1, n, S) = \max_{t \in \mathcal{T}(s)} p(t)$ , and backpointers  $bp$  which allow recovery of  $\arg \max_{t \in \mathcal{T}(s)} p(t)$ .

# Graph-based Dependency Parsing

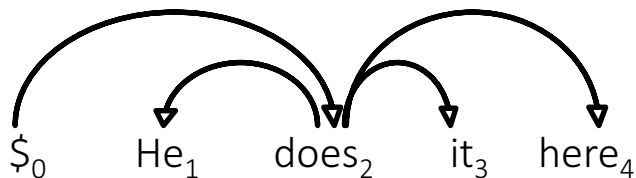
- Find the highest scoring tree from a complete dependency graph



$$Y^* = \arg \max_{Y \in \Phi(X)} \text{score}(X, Y)$$

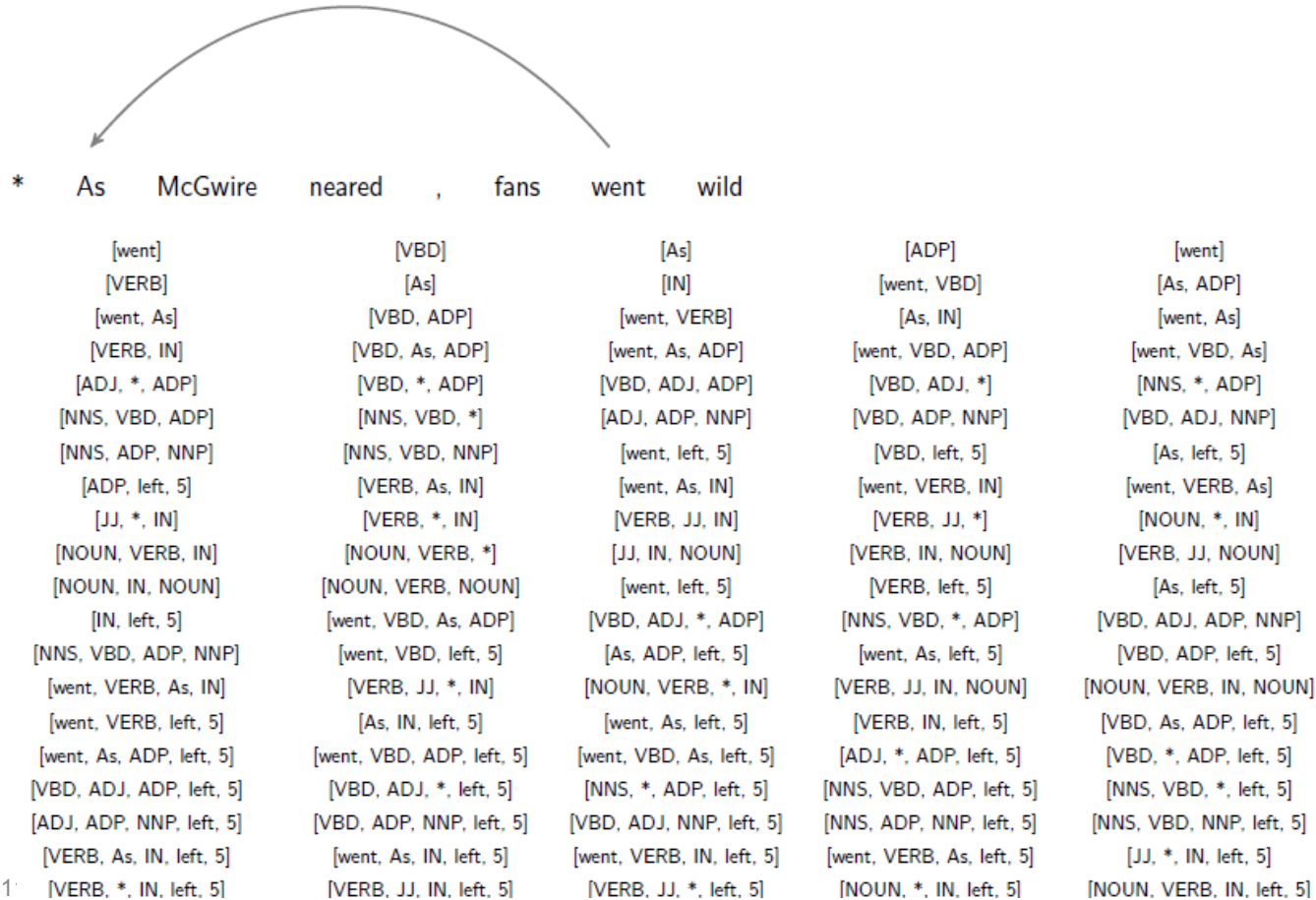
# First-order as an Example

- The first-order graph-based method assumes that arcs in a tree are independent from each other (arc-factorization)



$$score(X, Y) = \sum_{(h,m) \in Y} score(X, h, m)$$

# Features for an Arc



# Decoding for first-order model

- Maximum Spanning Tree (MST) Algorithm
- Eisner (2000) described a **dynamic programming** based decoding algorithm for bilexical grammar
- McDonald et al. (2005) applied this algorithm to the search problem of the second-order model
- Koo et al. (2010) investigate third-order model

# Part 3.2: Transition-based Methods

# Transition Systems



# A transition system

- Automata
  - State
    - Start state — an empty structure
    - End state — the output structure
    - Intermediate states — partially constructed structures
  - Actions
    - Change one state to another

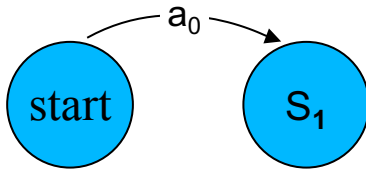
# A transition system

- Automata



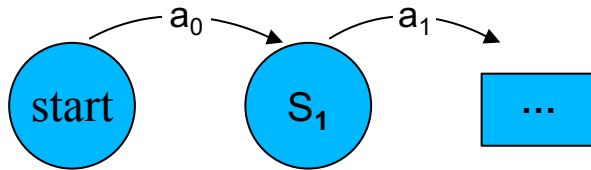
# A transition system

- Automata



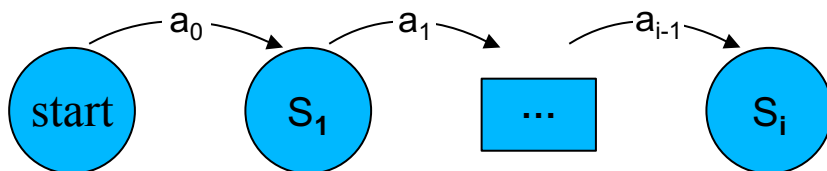
# A transition system

- Automata



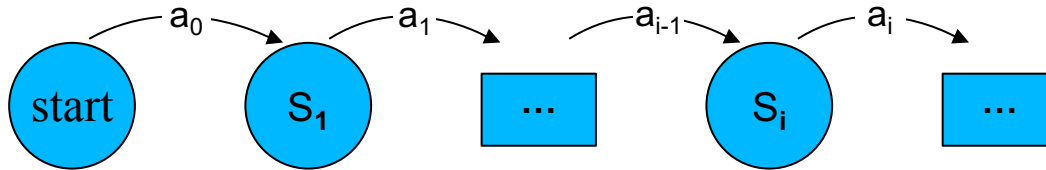
# A transition system

- Automata



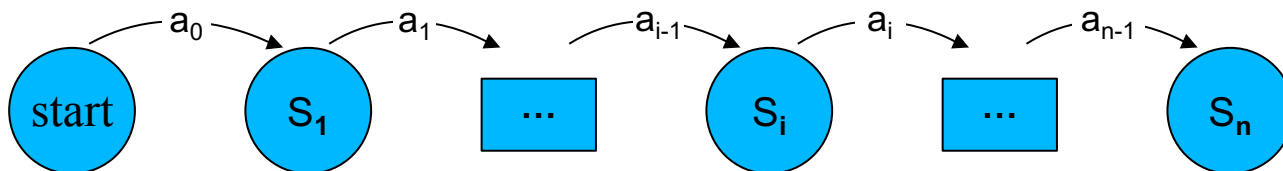
# A transition system

- Automata



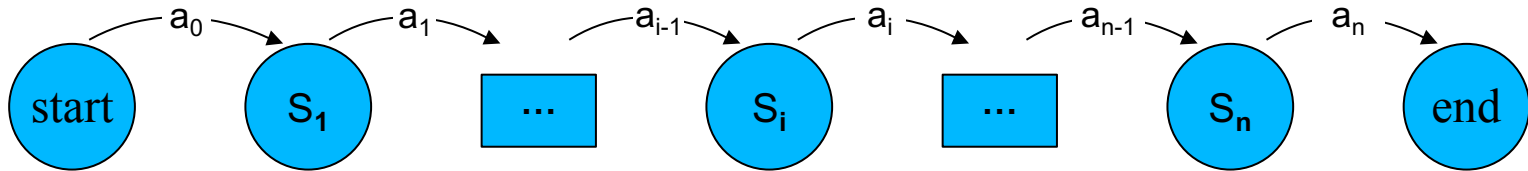
# A transition system

- Automata



# A transition system

- Automata

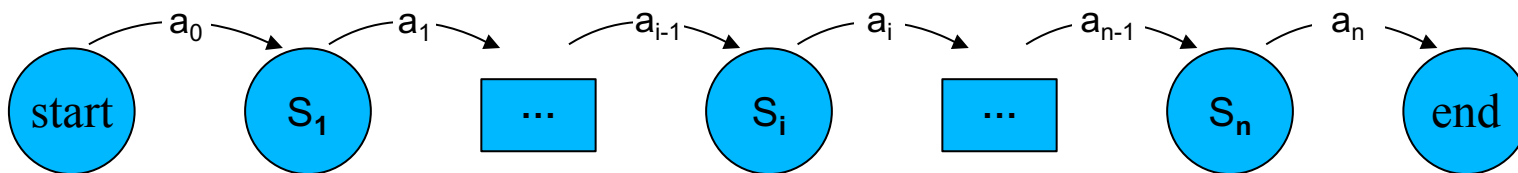




# A transition system

- State

- Corresponds to partial results during decoding
  - start state, end state,  $S_i$



- Actions

- The operations that can be applied for state transition
- Construct output incrementally

# Examples

# A transition-based POS-tagging example

- POS tagging

I like reading books → I/PRON like/VERB reading/VERB books/NOUN

- Transition system

- State

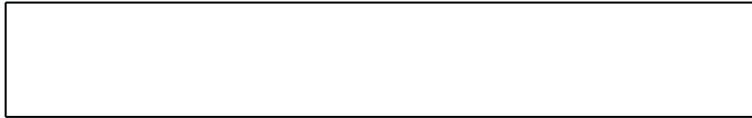
- Partially labeled word-POS pairs
    - Unprocessed words

- Actions

- TAG(t)  $w_1/t_1 \cdots w_i/t_i \rightarrow w_1/t_1 \cdots w_i/t_i w_{i+1}/t$

# A transition-based POS-tagging example

- Start State



I like reading books

# A transition-based POS-tagging example

- TAG(PRON)

I/PRON

like reading books

# A transition-based POS-tagging example

- TAG(VERB)

I/PRON like/VERB

reading books

# A transition-based POS-tagging example

- TAG(VERB)

I/PRON like/VERB reading/VERB

books

# A transition-based POS-tagging example

- TAG (NOUN)

I/PRON like/VERB reading/VERB books/NOUN



# A transition-based POS-tagging example

- End State

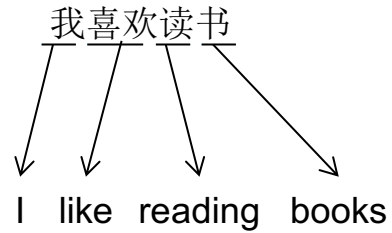
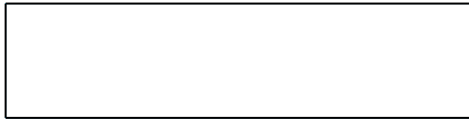
I/PRON like/VERB reading/VERB books/NOUN

# Word segmentation

- State
  - Partially segmented results
  - Unprocessed characters
- Two candidate actions
  - Separate    ## ## → ## ## #
  - Append      ## ## → ## ## #

# Word segmentation

- Initial State



# Word segmentation

- Separate

我

喜欢读书

# Word segmentation

- Separate

我 喜

欢读书

# Word segmentation

- Append

我 喜欢

读书

# Word segmentation

- Separate

我 喜欢 读

书

# Word segmentation

- Separate

我 喜欢 读 书



# Word segmentation

- End State

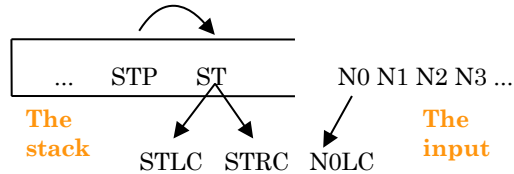
我 喜欢 读 书

# Transition-based Dependency Parsing

- State
  - A stack to hold partial structures
  - A queue of next incoming words
- Actions
  - SHIFT, REDUCE, ARC-LEFT, ARC-RIGHT

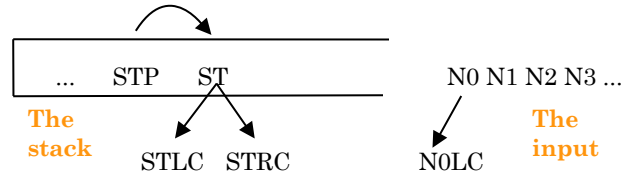
# Transition-based Dependency Parsing

- State



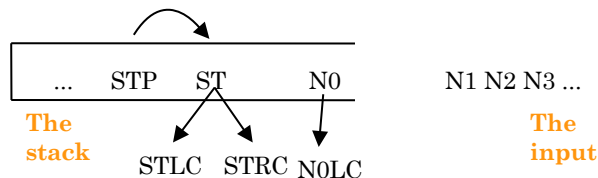
# Transition-based Dependency Parsing

- Actions
  - SHIFT



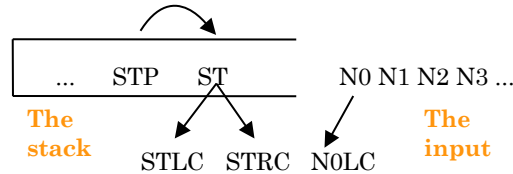
# Transition-based Dependency Parsing

- Actions
  - SHIFT



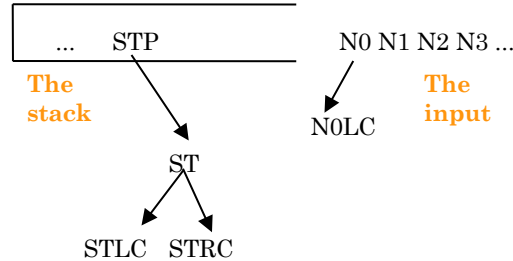
# Transition-based Dependency Parsing

- Actions
  - REDUCE



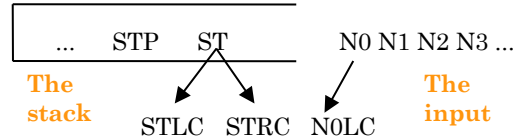
# Transition-based Dependency Parsing

- Actions
  - REDUCE



# Transition-based Dependency Parsing

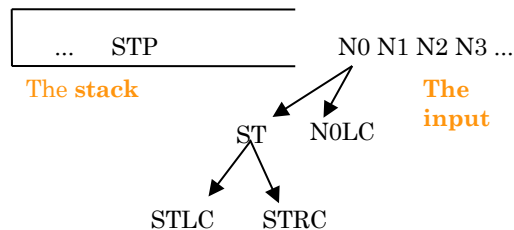
- Actions
  - ARC-LEFT





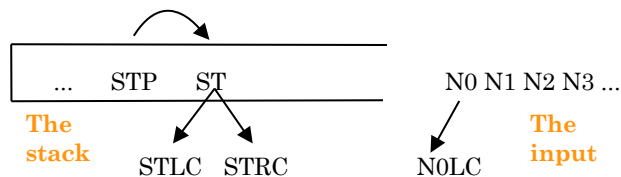
# Transition-based Dependency Parsing

- Actions
  - ARC-LEFT



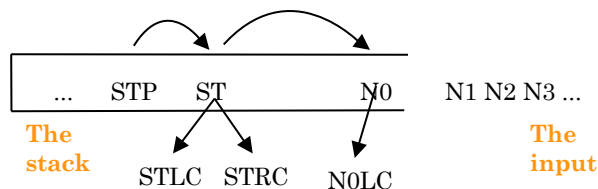
# Transition-based Dependency Parsing

- Actions
  - ARC-RIGHT



# Transition-based Dependency Parsing

- Actions
  - ARC-RIGHT



# Transition-based Dependency Parsing

- An Example
  - S-SHIFT
  - R-REDUCE
  - AL-ARC-LEFT
  - AR-ARC-RIGHT

He does it here

# Transition-based Dependency Parsing

- An Example

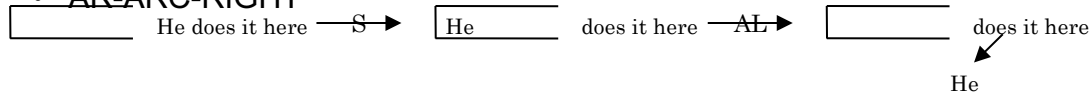
- S-SHIFT
- R-REDUCE
- AL-ARC-LEFT
- AR-ARC-RIGHT

He does it here —S→  He does it here

# Transition-based Dependency Parsing

- An Example

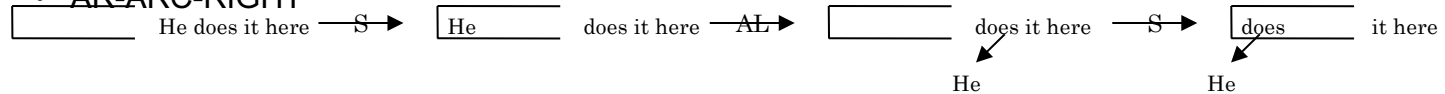
- S-SHIFT
- R-REDUCE
- AL-ARC-LEFT
- AR-ARC-RIGHT



# Transition-based Dependency Parsing

- An Example

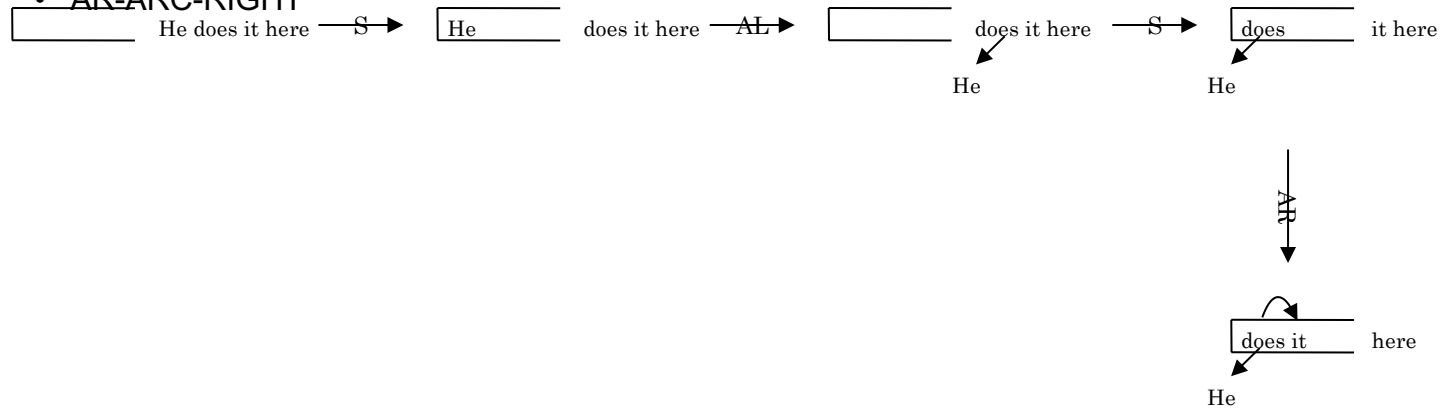
- S-SHIFT
- R-REDUCE
- AL-ARC-LEFT
- AR-ARC-RIGHT



# Transition-based Dependency Parsing

- An Example

- S-SHIFT
- R-REDUCE
- AL-ARC-LEFT
- AR-ARC-RIGHT

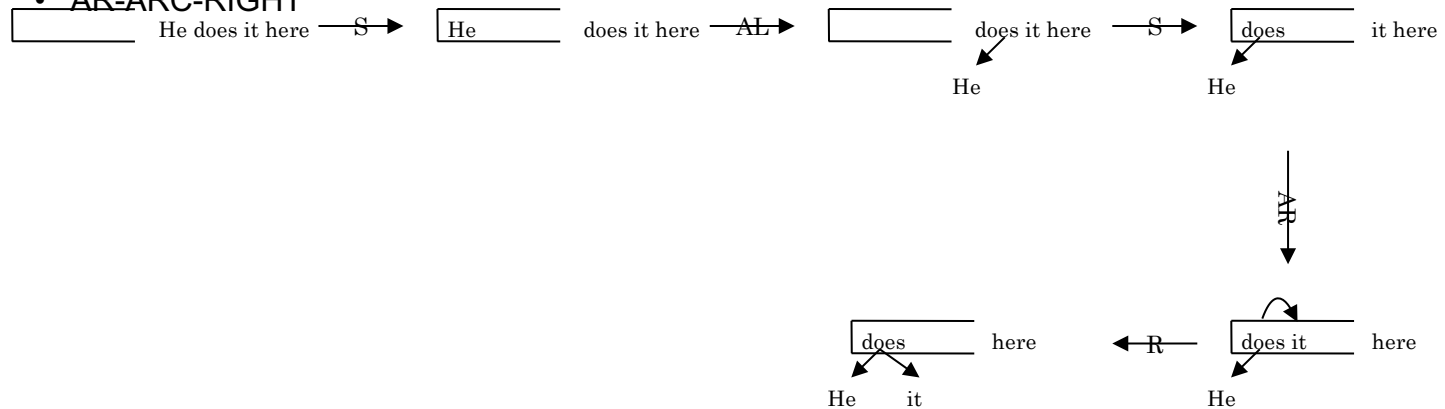




# Transition-based Dependency Parsing

- An Example

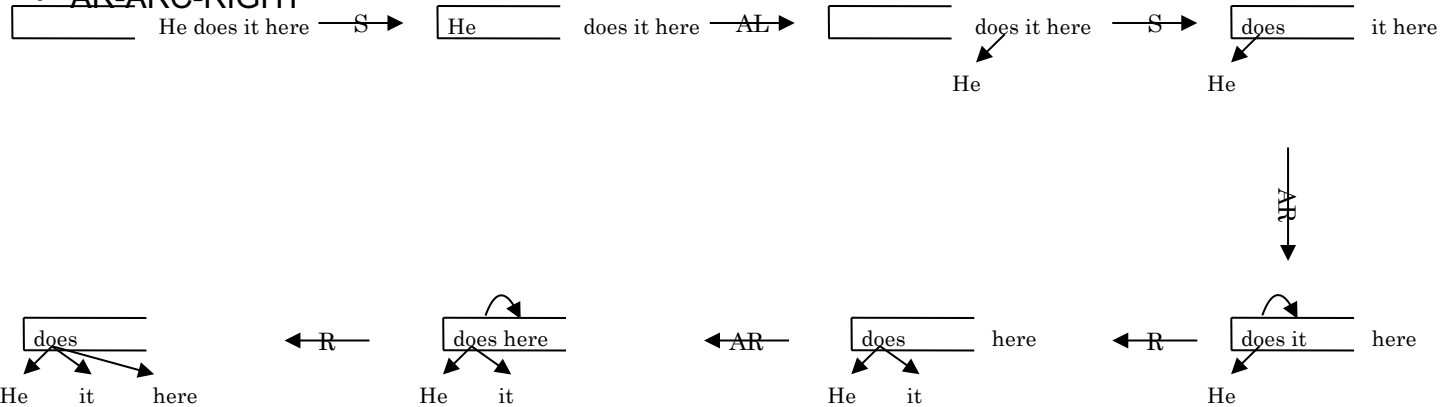
- S-SHIFT
- R-REDUCE
- AL-ARC-LEFT
- AR-ARC-RIGHT





# Transition-based Dependency Parsing

- An Example
  - S-SHIFT
  - R-REDUCE
  - AL-ARC-LEFT
  - AR-ARC-RIGHT



# Transition-based Constituent Parsing

- Actions
  - SHIFT

stack



queue

NR布朗 VV访问 NR上海

布朗(Brown) 访问(visits) 上海(Shanghai)

# Transition-based Constituent Parsing

- Actions
  - SHIFT

stack



queue

VV访问 NR上海

布朗(Brown) 访问(visits) 上海(Shanghai)

# Transition-based Constituent Parsing

- Actions
  - REDUCE-UNARY-X

stack



queue

VV访问 NR上海

布朗(Brown) 访问(visits) 上海(Shanghai)

# Transition-based Constituent Parsing

- Actions
  - REDUCE-UNARY-X

stack



queue

VV访问 NR上海

NR布朗

布朗(Brown) 访问(visits) 上海(Shanghai)

# Transition-based Constituent Parsing

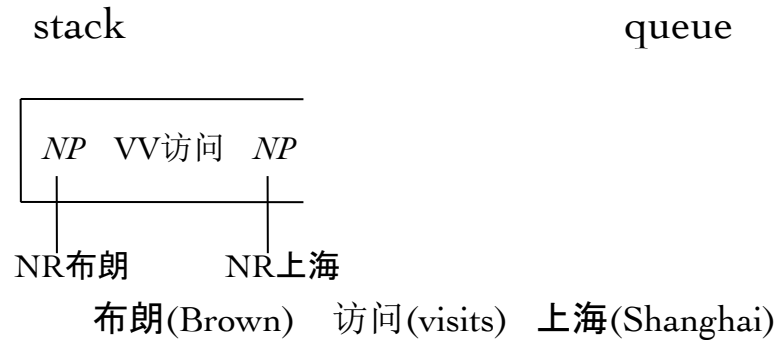
- Actions
  - REDUCE-UNARY-X





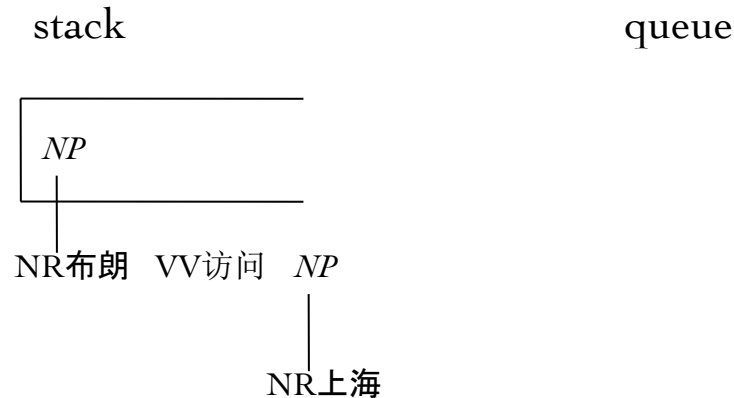
# Transition-based Constituent Parsing

- Actions
  - REDUCE-BINARY- $\{L/R\}$ -X



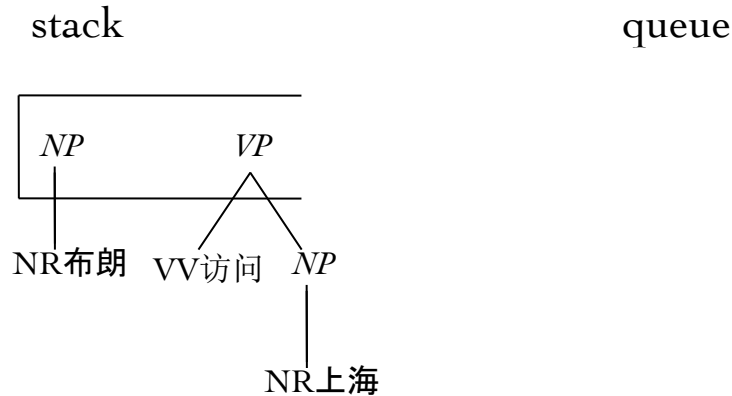
# Transition-based Constituent Parsing

- Actions
  - REDUCE-BINARY- $\{L/R\}$ -X



# Transition-based Constituent Parsing

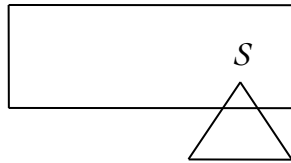
- Actions
  - REDUCE-BINARY- $\{L/R\}$ -X



# Transition-based Constituent Parsing

- Actions
  - TERMINATE

stack



queue

# Transition-based Constituent Parsing

- Actions
  - TERMINATE

stack



queue

ans



# Transition-based Constituent Parsing

- Example
  - SHIFT

stack

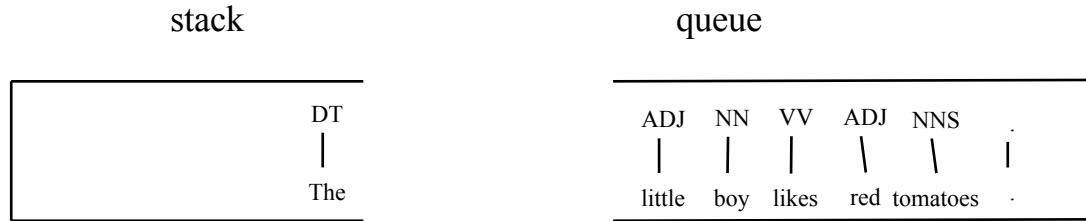


queue

DT	ADJ	NN	VV	ADJ	NNS	.
				\	\	
The	little	boy	likes	red	tomatoes	.

# Transition-based Constituent Parsing

- Example
  - SHIFT



# Transition-based Constituent Parsing

- Example
  - SHIFT

stack

	DT	ADJ
	The	little

queue

	NN	VV	ADJ	NNS	.
	boy	likes	red	tomatoes	.



# Transition-based Constituent Parsing

- Example
  - REDUCE-R-NP

stack

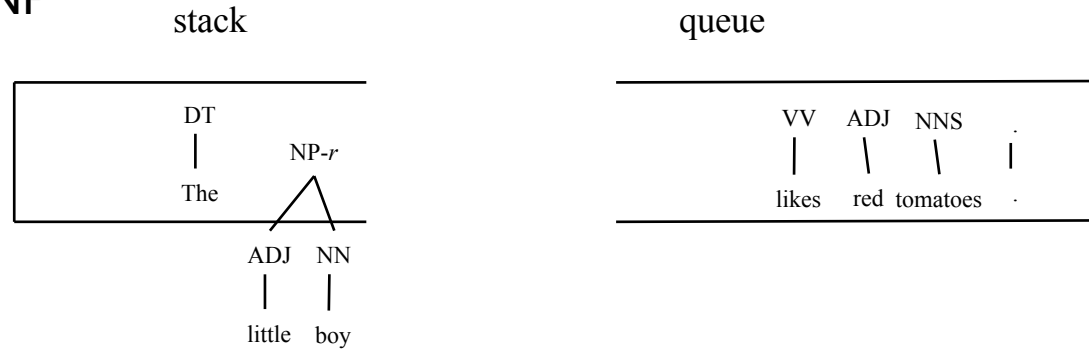
DT	ADJ	NN
The	little	boy

queue

VV	ADJ	NNS	.
likes	red	tomatoes	.

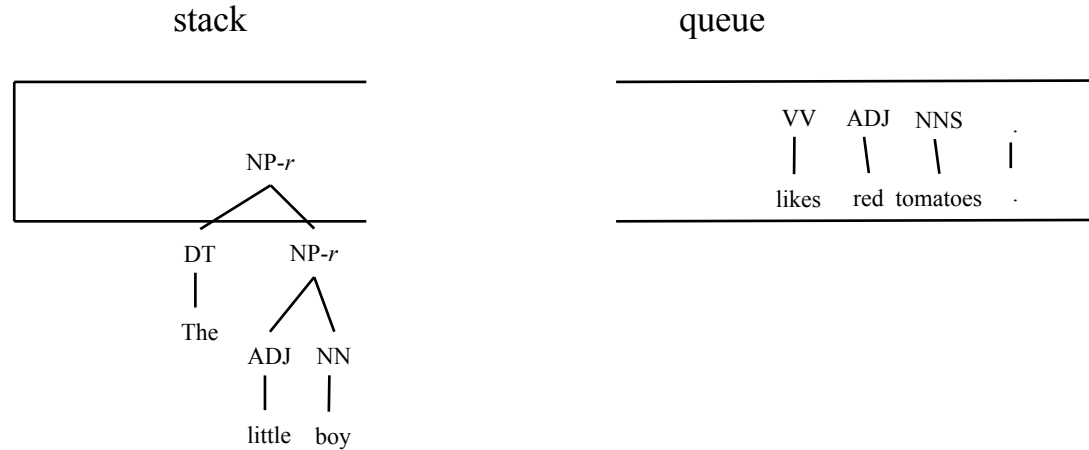
# Transition-based Constituent Parsing

- Example
  - REDUCE-R-NP



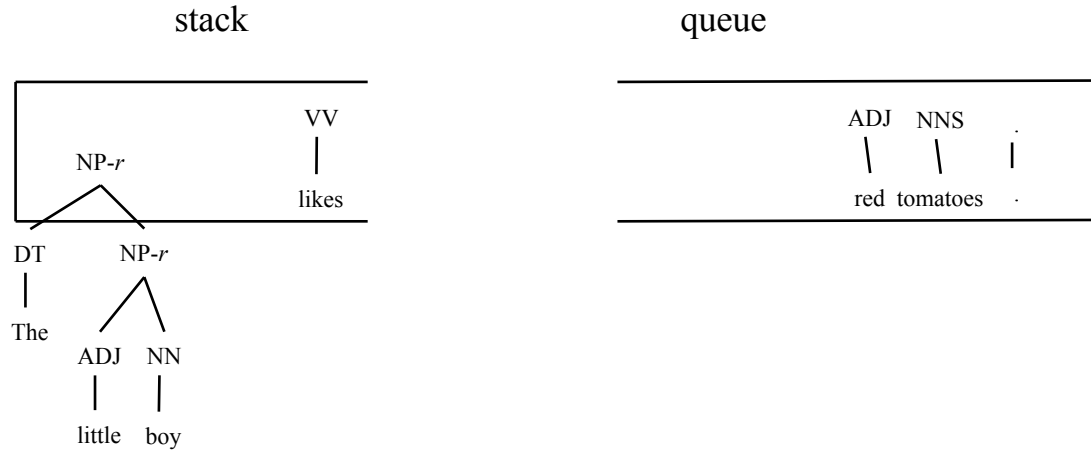
# Transition-based Constituent Parsing

- Example
  - SHIFT



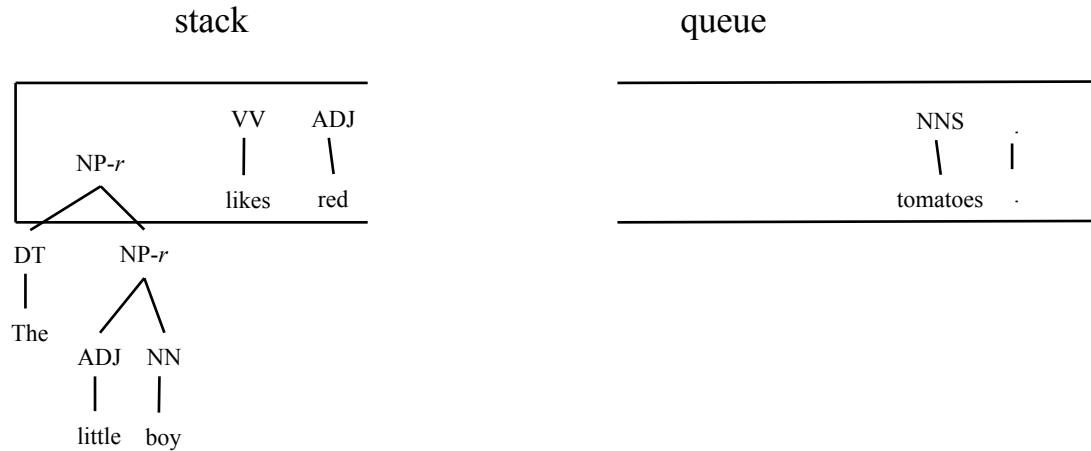
# Transition-based Constituent Parsing

- Example
  - SHIFT



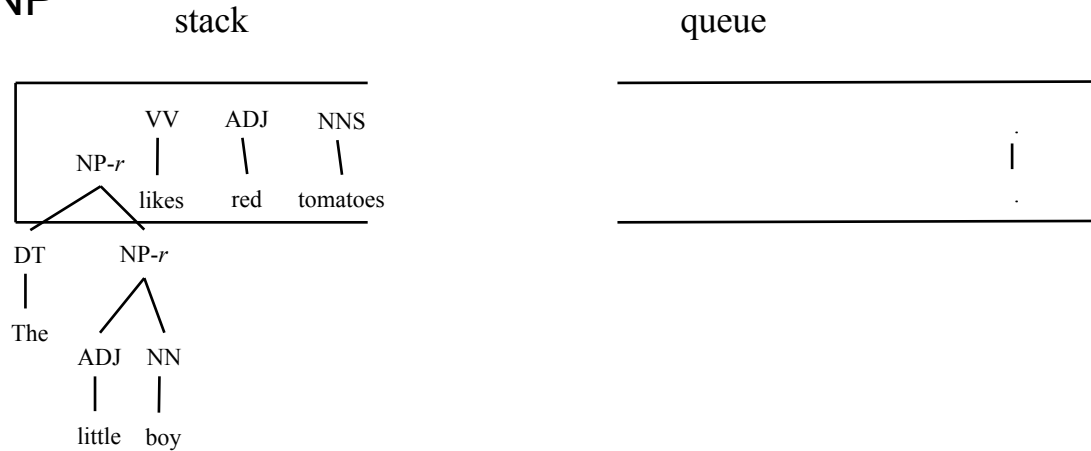
# Transition-based Constituent Parsing

- Example
  - SHIFT



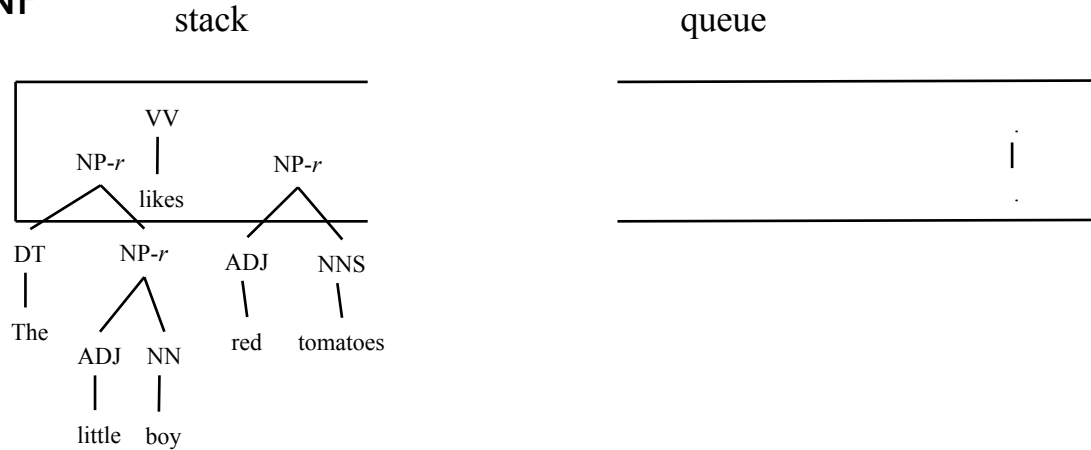
# Transition-based Constituent Parsing

- Example
  - REDUCE-R-NP



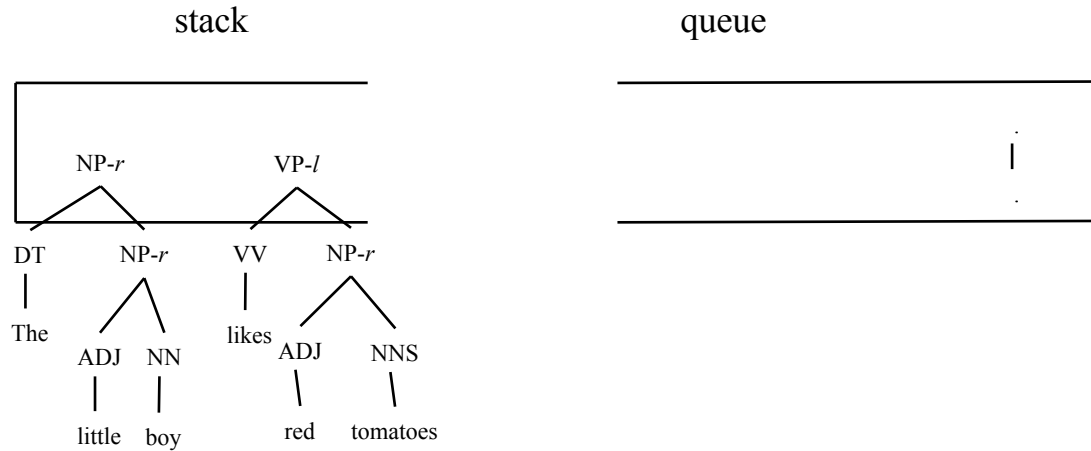
# Transition-based Constituent Parsing

- Example
  - REDUCE-L-NP



# Transition-based Constituent Parsing

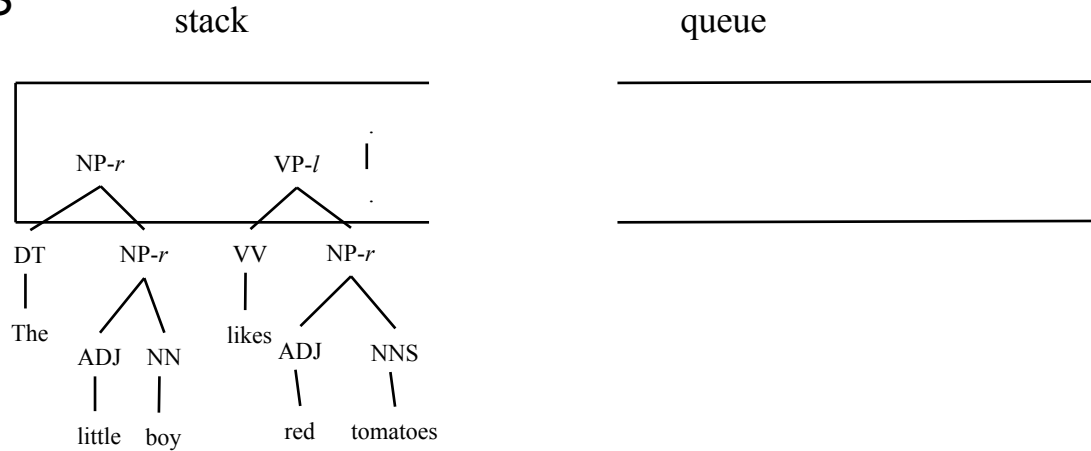
- Example
  - SHIFT





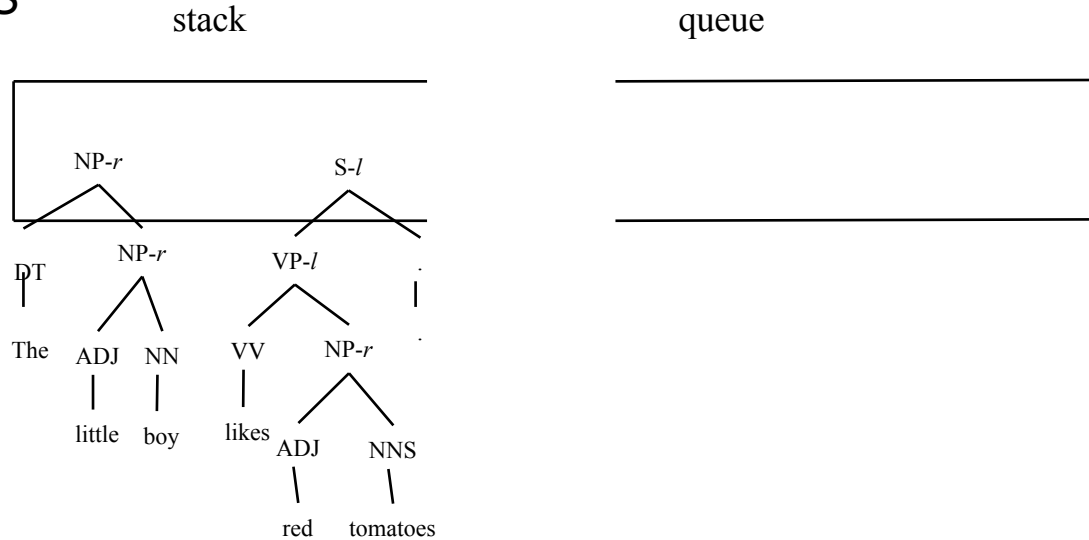
# Transition-based Constituent Parsing

- Example
  - REDUCE-L-S



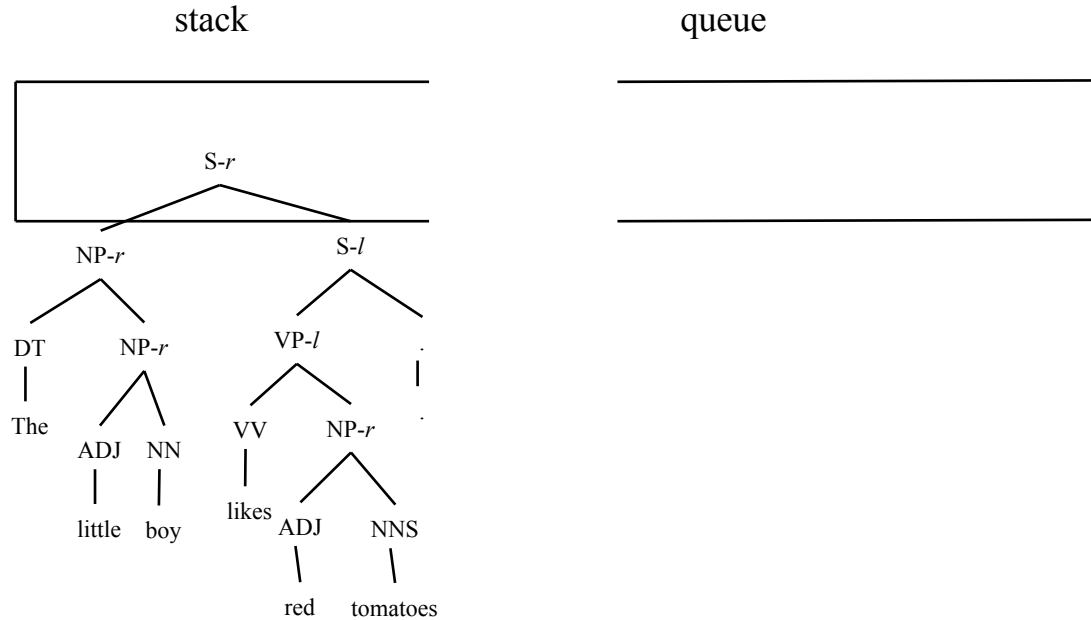
# Transition-based Constituent Parsing

- Example
  - REDUCE-R-S



# Transition-based Constituent Parsing

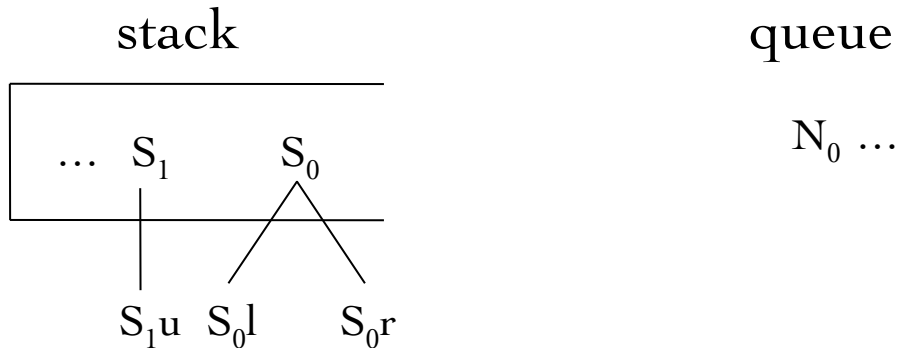
- Example
  - TERMINATE



Yue Zhang and Stephen Clark. 2011. *Syntactic Processing Using the Generalized Perceptron and Beam Search*. In *Computational Linguistics*, 37(1), March.

# Features

- Non-local Features
  - Extracted from top nodes on the stack  $S_0$ ,  $S_1$ ,  $S_2$ ,  $S_3$ , the left and right or single child of  $S_0$  and  $S_1$ , and the first words on the queue  $N_0$ ,  $N_1$ ,  $N_2$ ,  $N_3$ .



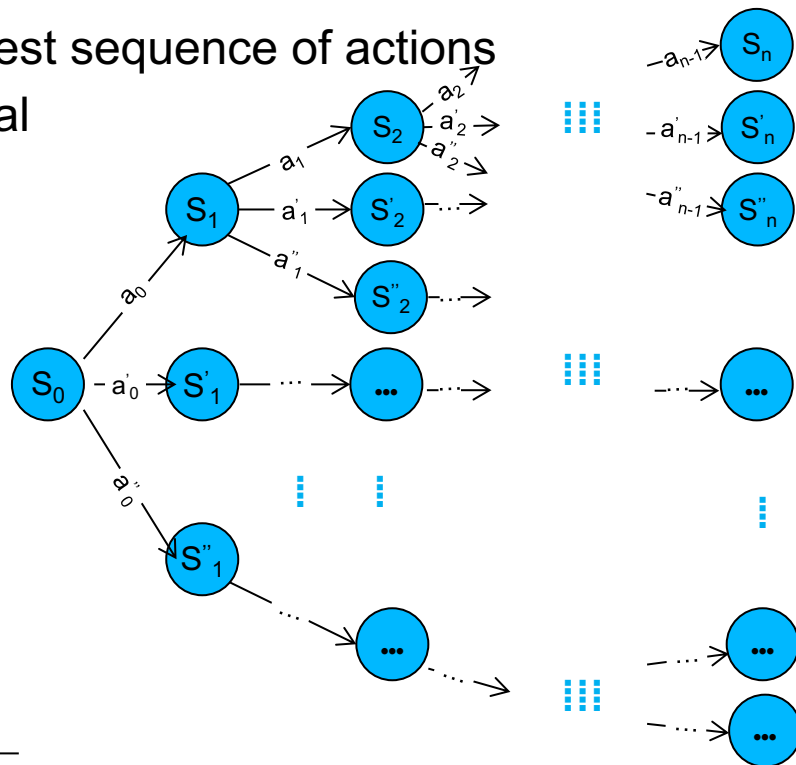
# Transition-based Methods

- Rich features
- Fast speed
- Search error

# Beam-search Decoding

# Search Space

- Find the best sequence of actions
- Exponential



# Beam-search decoding

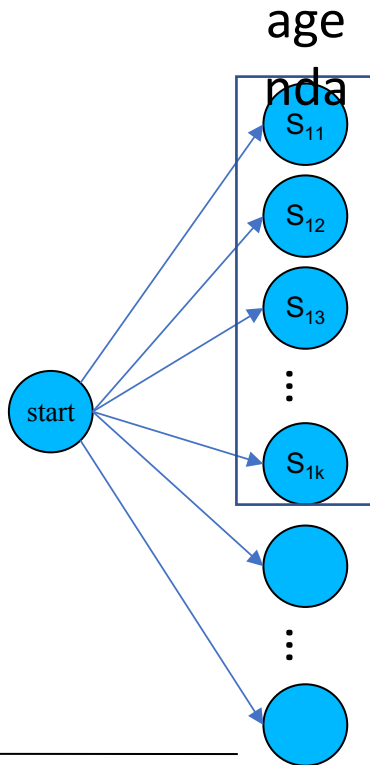


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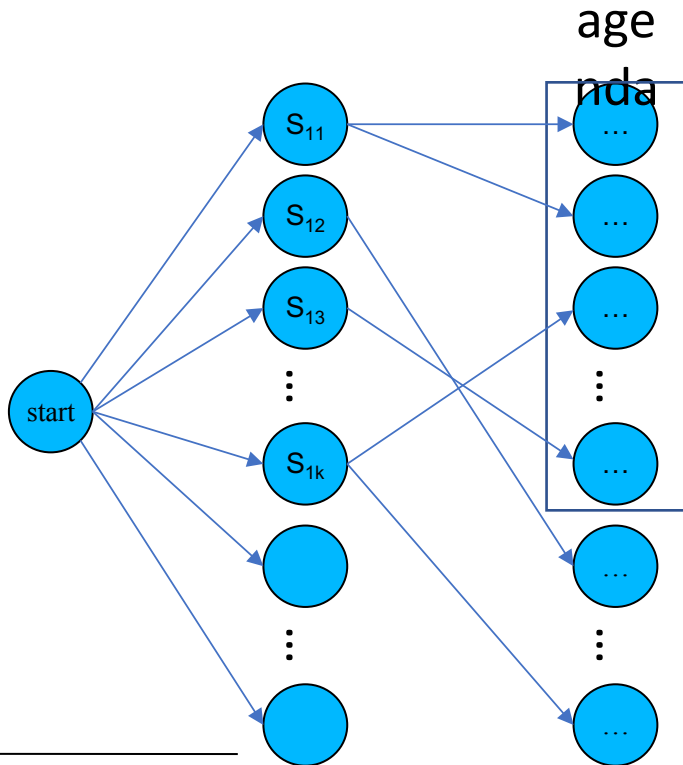


# Beam-search decoding



Yue Zhang and Stephen Clark. 2011. *Syntactic Processing Using the Generalized Perceptron and Beam Search*. In *Computational Linguistics*, 37(1), March.

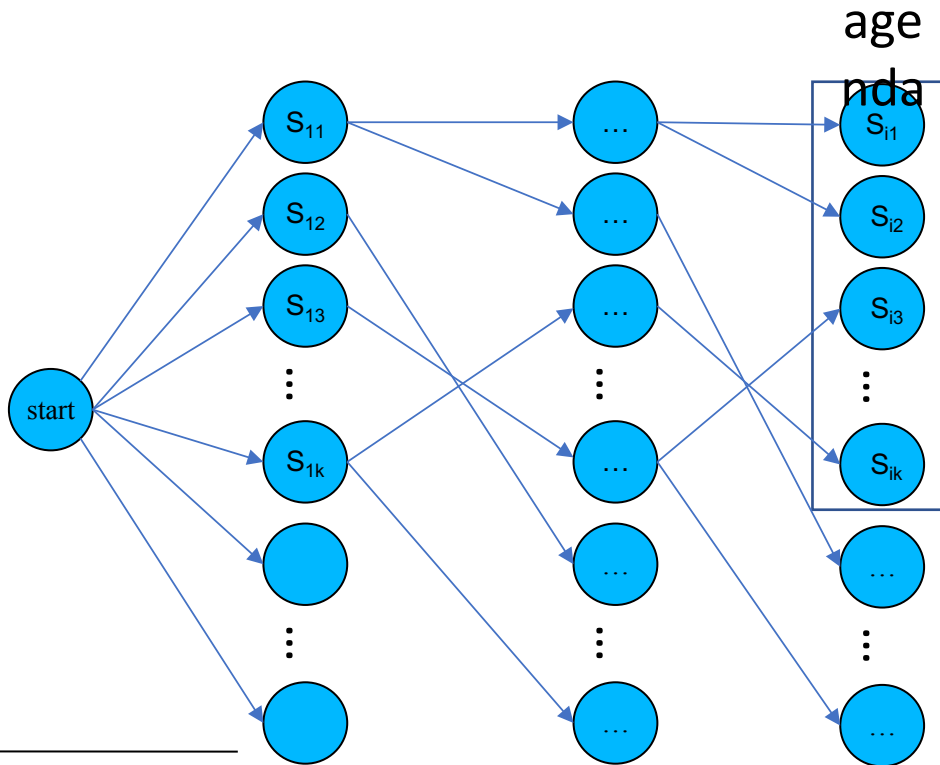
# Beam-search decoding



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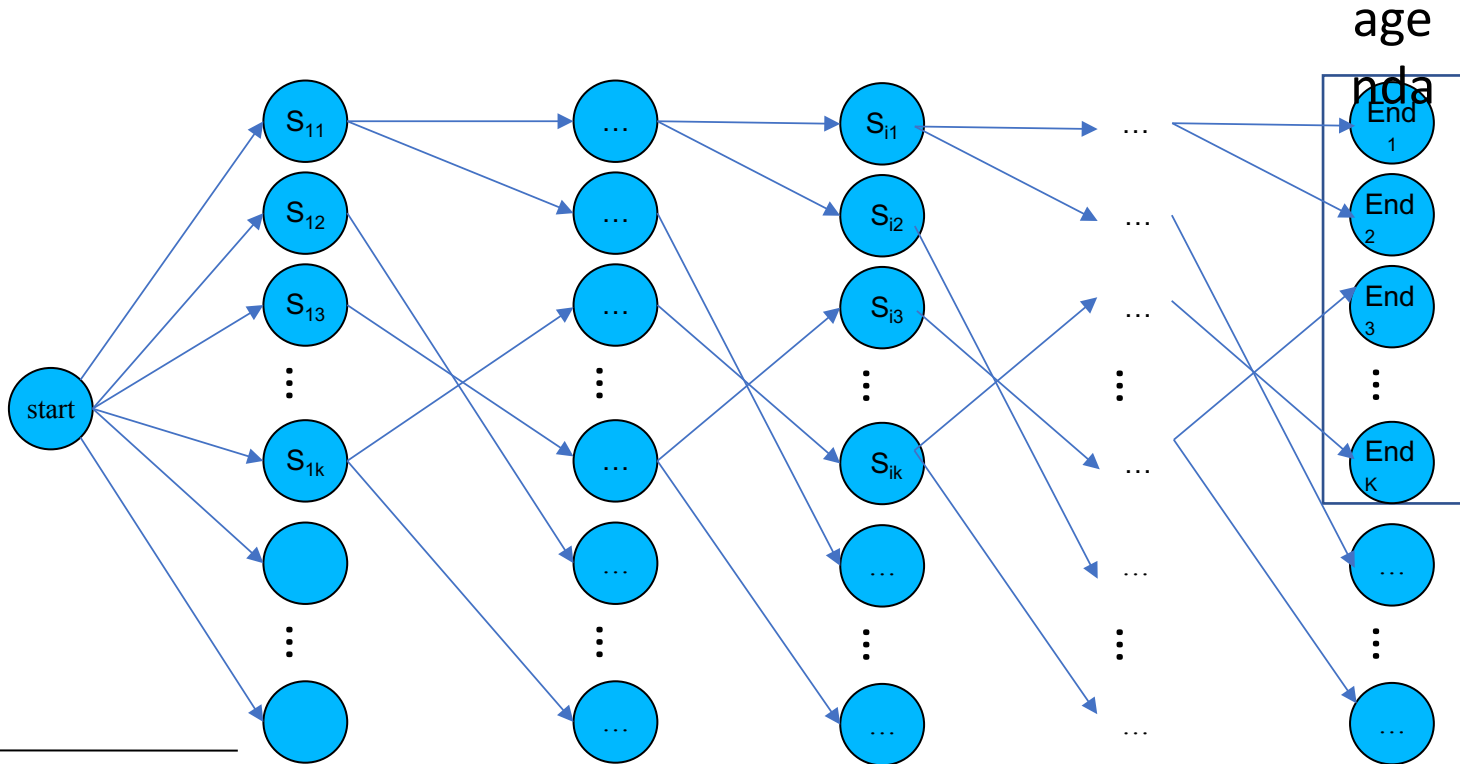
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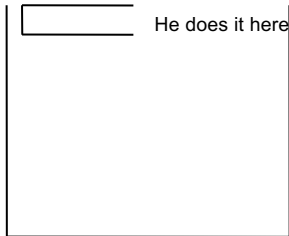
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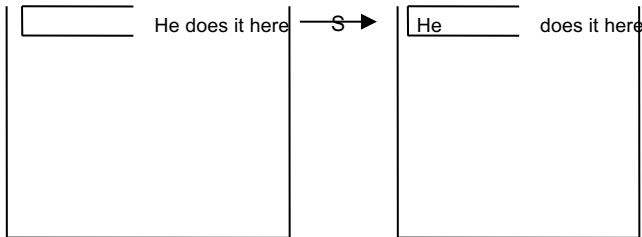
# Beam-search decoding

- Dependency Parsing Example
  - Decoding



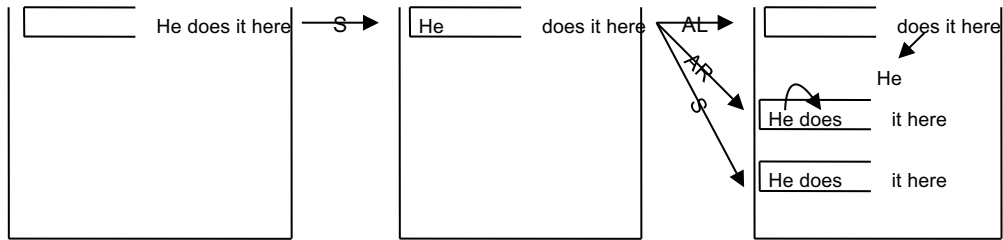
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- Dependency Parsing Example
  - Decoding



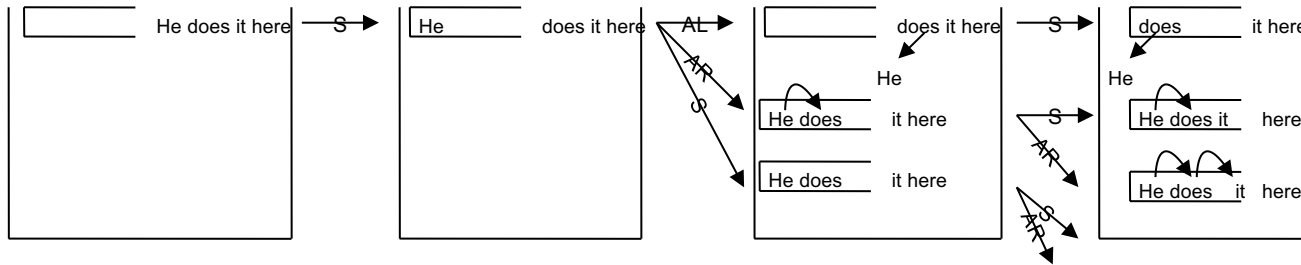
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- Dependency Parsing Example
  - Decoding



# Beam-search decoding

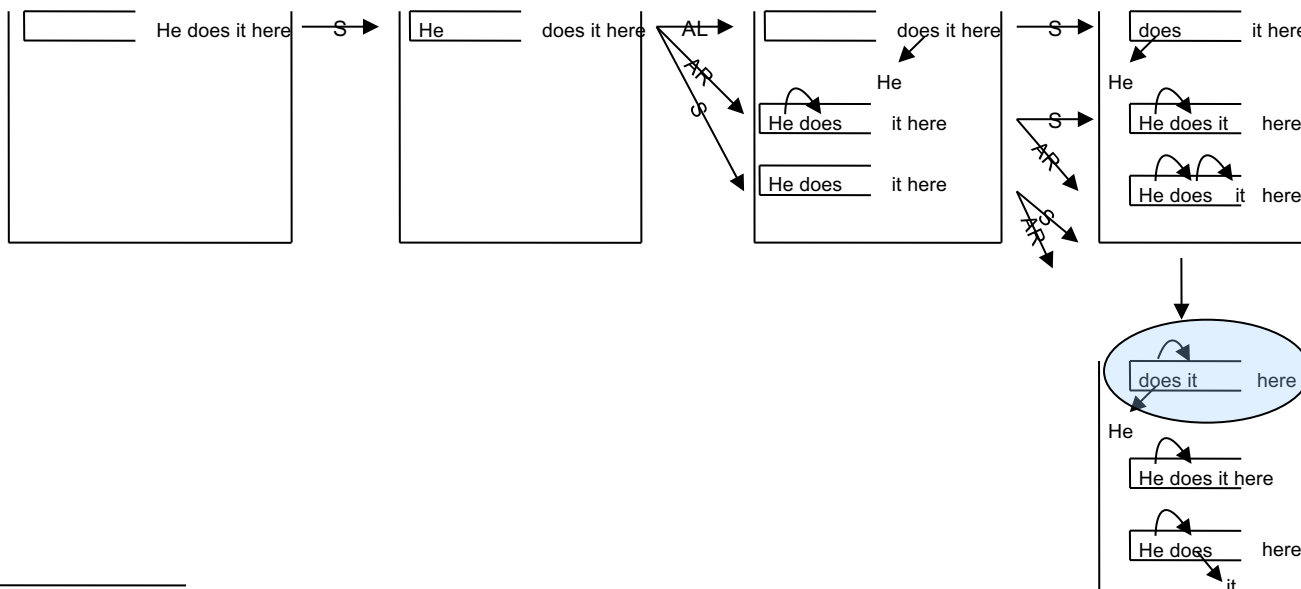
- Dependency Parsing Example
  - Decoding





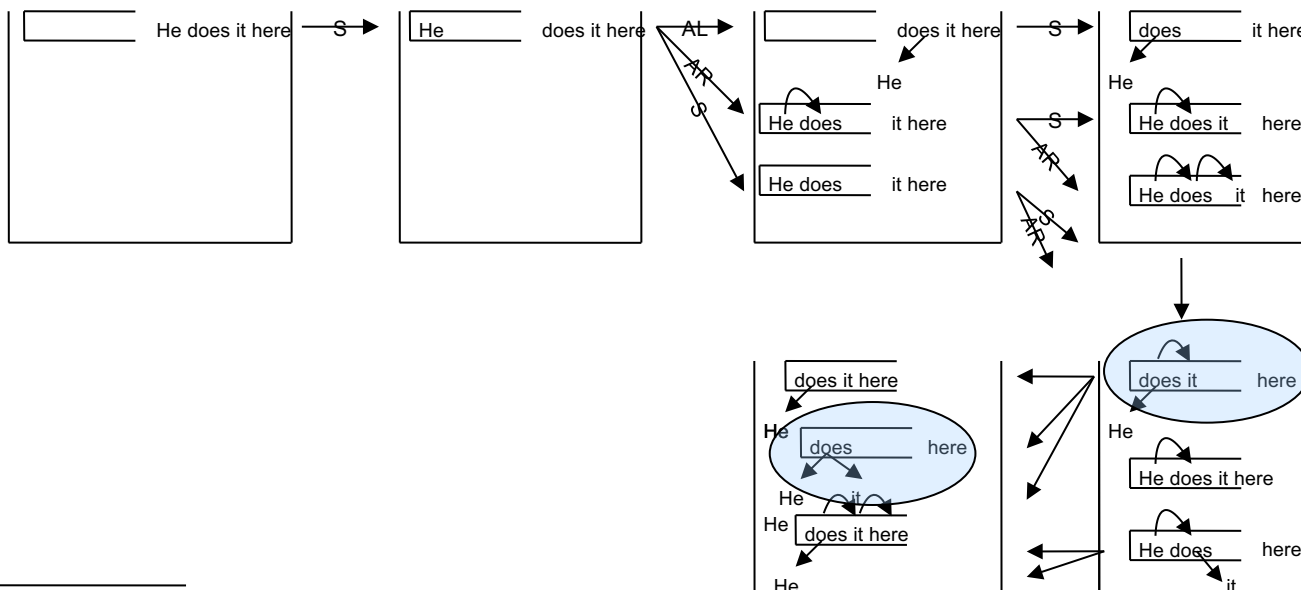
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  - Decoding



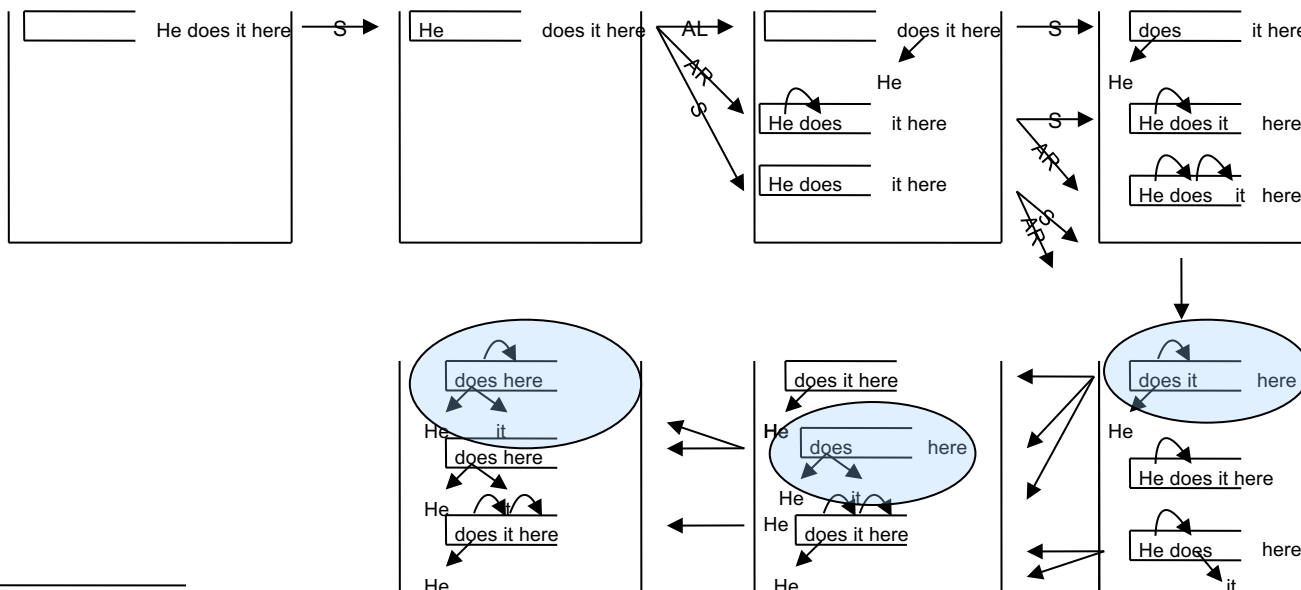
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  - Decoding



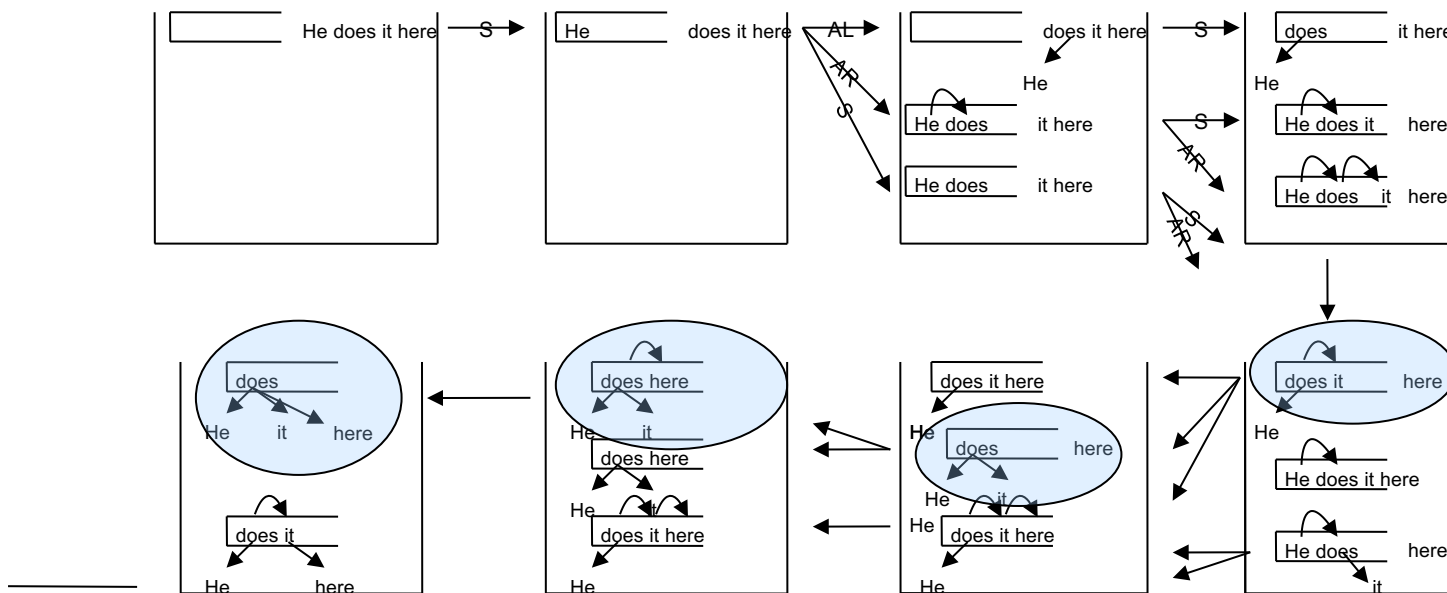
# Beam-search decoding

- Dependency Parsing Example
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# Beam-search decoding

**function** BEAM-SEARCH(*problem, agenda, candidates, B*)

*candidates* ← {STARTITEM(*problem*)}

*agenda* ← CLEAR(*agenda*)

**loop do**

**for each** *candidate* **in** *candidates*

*agenda* ← INSERT(EXPAND(*candidate, problem*), *agenda*)

*best* ← TOP(*agenda*)

**if** GOALTEST(*problem, best*)

**then return** *best*

*candidates* ← TOP-B(*agenda, B*)

*agenda* ← CLEAR(*agenda*)

# Global Training

# Structured Learning

- Model **whole sequences** of actions
  - Correspond to structures

# Learning guided search

- Search not optional (vs graph-based structured prediction)
- Learn to fix search errors

